



# Chap10 Direct-Current (DC) Circuits

# Electric Current

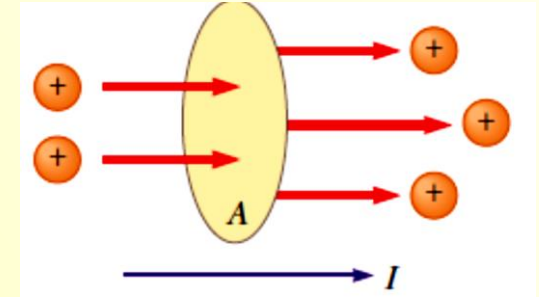
... scalar

- the rate at which charge flows through a surface.

- Magnitude: 
$$I = \frac{\Delta Q}{\Delta t}$$

- SI unit: A [1 A = 1 C/s]

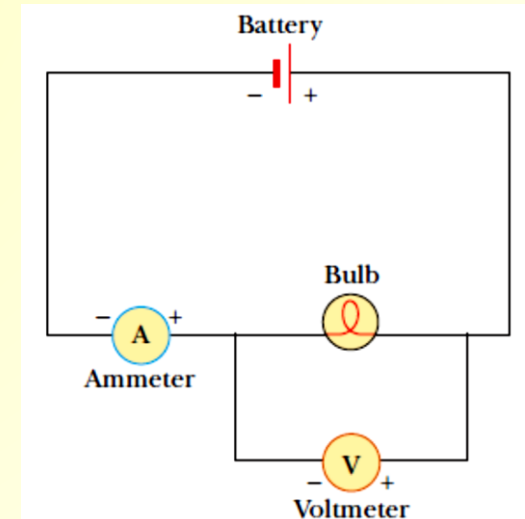
- Direction: the direction in which *positive charges* flow.



# Voltage

... scalar

- The difference in electric potential between two points, which creates a current in a closed circuit.
- SI unit: V



# Resistance

... *scalar*

- The resistance of an object depends on the material it is made of and its shape.

- Definition:  $R \equiv \frac{\Delta V}{I}$

- SI unit:  $\Omega$  [ $1 \Omega = 1 \text{ V/A}$ ]

- Ohm's law:  $\Delta V = IR$

- Resistance of an ohmic conductor:

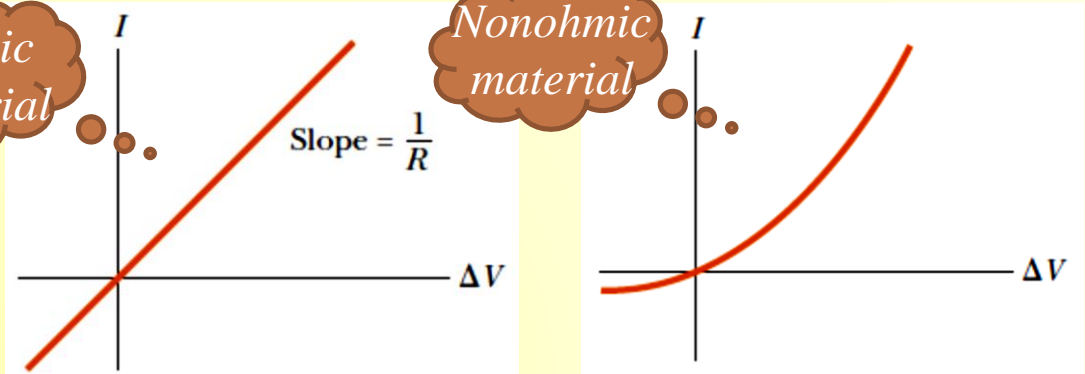
$$R = \rho \frac{l}{A}$$

$\rho$ : the resistivity of the material

$l$ : the conductor's length

$A$ : the conductor's cross-sectional area

- Resistivity of a material depends on its molecular & atomic structure and on temperature.



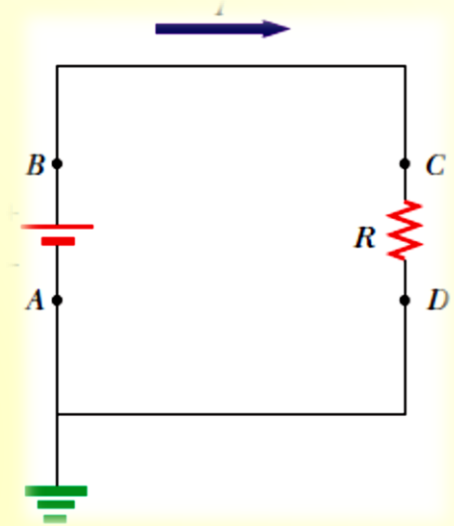
# Electric Energy & Power

## ➤ Electric power: ... *scalar*

- Magnitude:  $P = I\Delta V$
- SI unit: W [1 W = 1 V·A]
- As for ohmic resistors:

$$P = I^2 R = \frac{\Delta V^2}{R}$$

- The light intensity of a light bulb is related to its power.



## ➤ Electric energy: ... *scalar*

- Magnitude:  $E = Pt$
- SI unit: J [1 J = 1 W·s], Common unit: kWh [1 kWh =  $3.6 \times 10^6$  J]

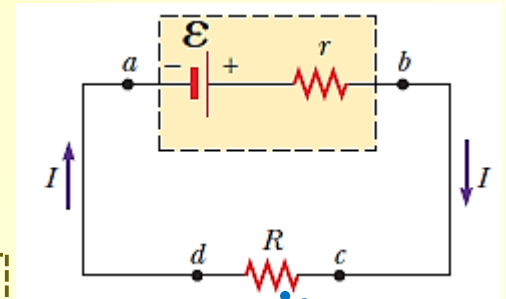
# Sources of EMF

## ➤ EMF:

- EMF ( $\varepsilon$ ) stands for “*Electromotive Force*”, but it is not a force, it is the work done (increase of electric potential energy) per unit charge.
- SI unit: volt (V)

## ➤ Internal Resistance:

- Internal resistance ( $r$ ) is the resistance of a battery or a generator.
- Internal resistance subtracts voltage from the EMF, and the residual voltage is called the terminal voltage.
- The terminal voltage of the battery:  $\Delta V = \varepsilon - Ir$



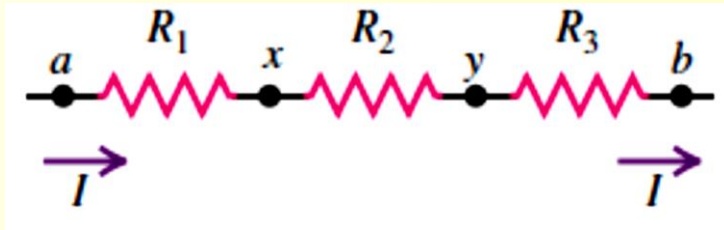
load resistance

$$\left. \begin{array}{l} \varepsilon = \Delta V + Ir \\ \Delta V = IR \end{array} \right\} \Rightarrow \varepsilon = IR + Ir \Rightarrow \varepsilon I = I^2 R + I^2 r$$

Power output of emf source

# Combinations of Resistors

## ➤ In series:



- Resistance adds:

$$R_s = R_1 + R_2 + R_3 + \dots$$

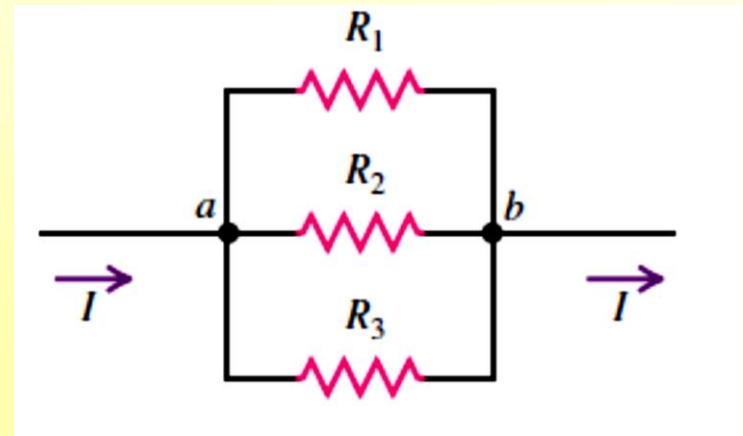
- Current remains the same:

$$I_s = I_1 = I_2 = I_3 = \dots$$

- Voltage adds:

$$V_s = V_1 + V_2 + V_3 + \dots$$

## ➤ In parallel:



- The reciprocal of resistance adds:

$$\frac{1}{R_p} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots$$

- Current adds:

$$I_p = I_1 + I_2 + I_3 + \dots$$

- Voltage remains the same:

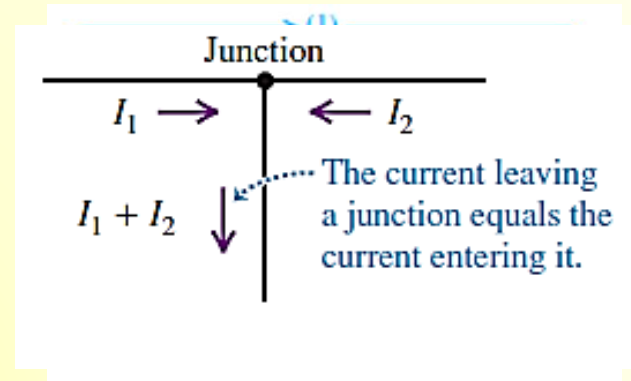
$$V_p = V_1 = V_2 = V_3 = \dots$$

# Complex Circuits & Kirchhoff's Rules

## ➤ Junction rule:

Conservation of charge

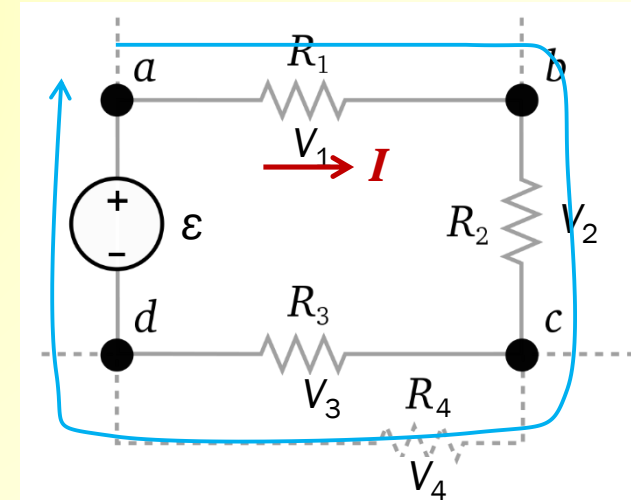
- The sum of the currents entering any junction must equal the sum of the currents leaving that junction.



## ➤ Loop rule:

Conservation of energy

- The sum of the potential differences across all the elements around any closed circuit loop must be zero.
- Loop *abcd*:  $-V_1 - V_2 - V_3 + \varepsilon = 0$

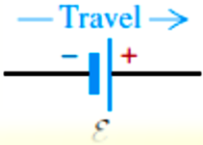


- Sign Conventions for the Loop Rule:

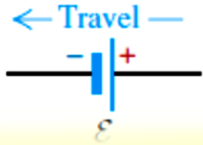
Potential drops “-”  
Potential increases “+”

a) Sign conventions for emfs

+ $\mathcal{E}$ : Travel direction from - to +:



- $\mathcal{E}$ : Travel direction from + to -:

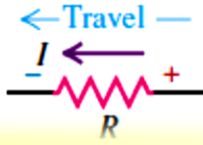


(b) Sign conventions for resistors

+ $IR$ : Travel opposite to current direction:



- $IR$ : Travel in current direction:



In each part of the figure “Travel” is the direction that we imagine going around the loop, which is not necessarily the direction of the current.

**【Exercise】**

Find  $I_1$ ,  $I_2$ , and  $I_3$  in the right Figure.

Junction  $c$ :  $I_3 = I_1 + I_2$

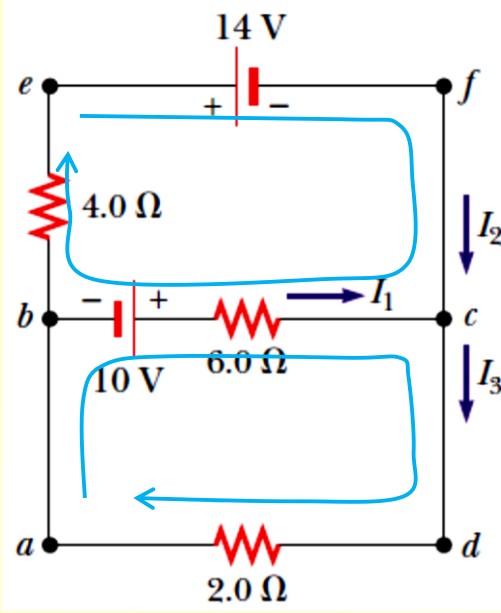
Loop  $abcd$ :

$$10\text{V} - (6.0\Omega)I_1 - (2.0\Omega)I_3 = 0$$

Loop  $efcbe$ :

$$-14\text{V} + (6.0\Omega)I_1 - 10\text{V} - (4.0\Omega)I_2 = 0$$

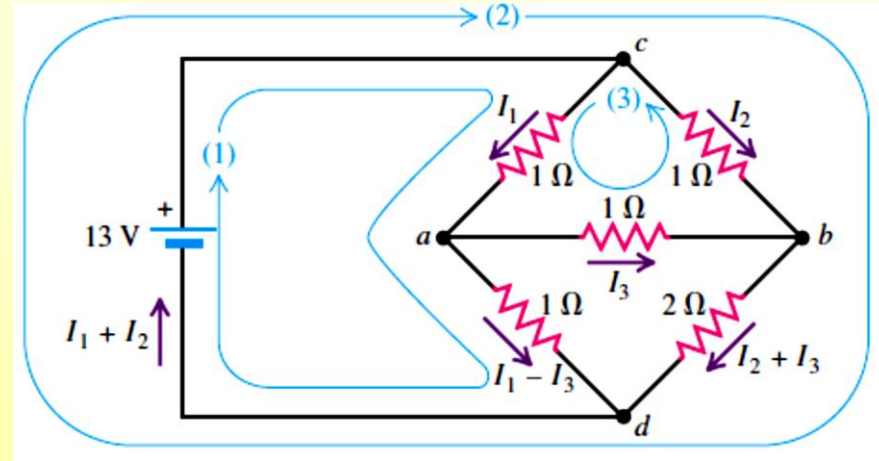
$$\left. \begin{array}{l} I_1 = 2.0\text{A} \\ I_2 = -3.0\text{A} \\ I_3 = -1.0\text{A} \end{array} \right\}$$





## 【Exercise】 A complex network

The right figure shows a “bridge” circuit. Find the currents  $I_1$ ,  $I_2$ , and  $I_3$  and the equivalent resistance of the network of five resistors.



**Loop (1):**

$$-(1\Omega)I_1 - (1\Omega)(I_1 - I_3) + 13V = 0$$

**Loop (2):**

$$-(1\Omega)I_2 - (2\Omega)(I_2 + I_3) + 13V = 0$$

**Loop (3):**

$$-(1\Omega)I_1 - (1\Omega)I_3 + (1\Omega)I_2 = 0$$



$$\begin{cases} I_1 = 6A \\ I_2 = 5A \\ I_3 = -1A \end{cases}$$

**Equivalent resistance of the network:**  $R_{eq} = \frac{13V}{I_1 + I_2} = \frac{13V}{11A} \approx 1.2\Omega$